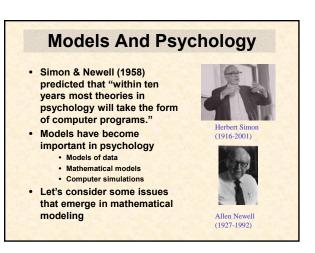
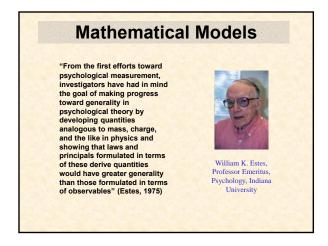
# Psychology 452 Week 5: Perceptrons And Animal Learning •Mathematical Models •Mathematical Models Of Conditioning •Rescorla-Wagner •Logical Neuron •Equivalence Between Models •Empirical •Formal •The Perceptron Paradox

Course Trajectory			
When	What		
Weeks 1-3	Basics of three architectures (DAM, perceptron, MLP)		
Weeks 4-6	Cognitive science of DAMs and perceptrons		
Week 7	Connectionism and Cognitive Psychology		
Weeks 8-10	Interpreting MLPs		
Weeks 11-13	Case studies (interpretations, applications, architectures)		







Prope	erties	
Property	Mathematical Models	
Analyses of existing data	Yes	
Linear transformation	Usually not	
Goodness of fit	Yes	
Yields surprises	Maybe	
Behaves	No	

#### Hull's Law For Growth Of S-R Habits

- "The essential nature of the learning process may, however, be stated quite simply... the process of learning consists in the strengthening of certain of these connections as contrasted with others, or in the setting up of quite new connections" (Hull, 1943).
- The physiological limit or maximum
- $I_S^{-}R_I$ . The constant factor (f) according to which a portion ( $\Delta_S^+H_R^-$ ) of the unrealized potentiality is transferred to the actual habit strength at a given reinforcement.
- · Over trials, the law becomes:

$$\Delta_S H_R = f(M - _S H_R)$$

 ${}_{S}^{N}\boldsymbol{H}_{R} = \boldsymbol{M} - \boldsymbol{M}\boldsymbol{e}^{-N\log(\frac{1}{1-f})}$ 

# **Pavlovian Conditioning**

- Pavlovian conditioning is the process of repeatedly pairing a CS with an US so that eventually the CS will produce this response
- We can gain tremendous insights into this type of learning by considering mathematical equations that attempt to account for it



Before conditioning....

Food (US) --> Salivation (UCR)

Bell (CS) ---> No Salivation

After conditioning....

Bell (CS) ---- > Salivation (CR)

# **Conditioning And Context**

- · CS does not occur in a vacuum
- · CS appears in the context of numerous other stimuli
- Context, and previous training, can interfere with the desired learning of the CS
- · This is nicely demonstrated by Kamin's blocking phenomenon



Leon J. Kamin

# **Blocking Phenomenon**

- If CS<sub>1</sub> (the bell) has already been conditioned to elicit the response, then when it is paired with CS2 (the light), further learning does not occur
- CS<sub>1</sub> blocks the learning (conditioning) that could have occurred with CS2!

Two Phase Experimental Condition Bell Food Bell Light

One Phase Control Condition

Bell Light Food

# **Explaining Blocking**

"Organisms only learn when events violate their expectations. Certain expectations are built up about events following a stimulus context; expectations initiated by the complex and its component stimuli are then only modified when consequent events disagree with the composite expectation" (Rescorla & Wagner, 1972)





# Rescorla-Wagner Rule

- Rescorla and Wagner used a mathematical model to make their "cognitive" account more  $\Delta V_{(t)} = \alpha \Big(\lambda - V_{(t)}\Big)$ 
  - rigorous
  - ΔV<sub>(t)</sub> Change in associative strength at time t V<sub>(t)</sub> - Current associative
  - strength of CS α - Salience of CS
  - λ Maximum associative strength possible

Food

# **Multiple CSs**

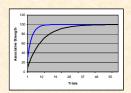
- The Rescorla-Wagner model can easily be generalized to handle situations in which more than one CS can be presented
- This is done by assuming that there is a total associative strength that is the sum of the components, and that the Rescorla-Wagner equation can be selectively applied to each CS

$$\Sigma V = V_A + V_B + V_C$$

$$\Delta V_{A(t)} = \alpha_A \left( \lambda - \Sigma V_{(t)} \right)$$

# Formalizing Learning

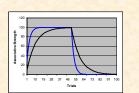
- The Rescorla-Wagner model works by choosing values for the constants, and updating associative strength if the CS is present
- For both runs on the right, λ = 100
- For the blue line,  $\alpha = 0.3$ , and for the black line  $\alpha = 0.3$



$$\Delta V_{A(t)} = \alpha_A \left( \lambda - \Sigma V_{(t)} \right)$$

# **Formalizing Extinction**

- Extinction is modeled by changing the value of λ to 0 in the weight change equation
- The examples on the right continue the previous example, extinguishing the conditioning from Phase 1

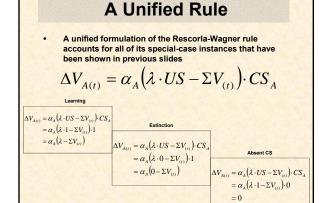


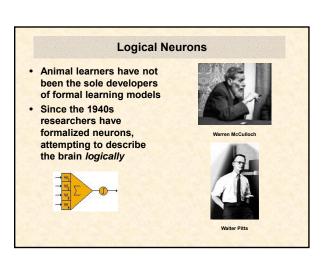
$$\Delta V_{A(t)} = \alpha_A \left( 0 - \Sigma V_{(t)} \right)$$

# **Formalizing CS Absence**

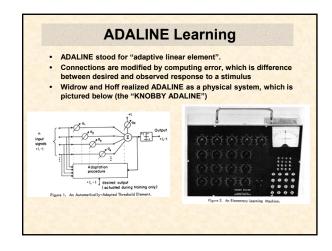
- The associative strength is not always modified
- If the CS is not presented, then its associative strength will not change
- The equation below bluntly defines this situation

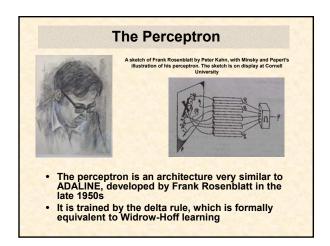
$$\Delta V_{A(t)} = 0$$

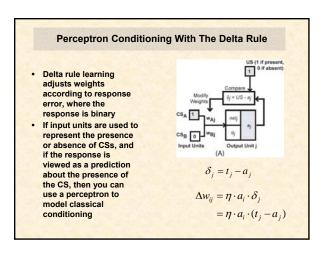


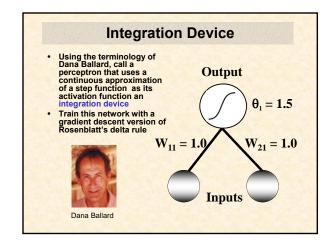


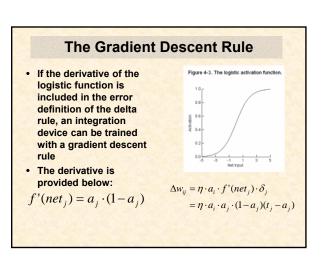
# Formal Neurons Learn Some logical neurons, like the ADALINE model developed by Widrow and Hoff in 1959, learn Feedback about the correctness of their responses is used to modify connection weights Formal Neurons Bernard Widrow Microw Widrow Marcian Hoff

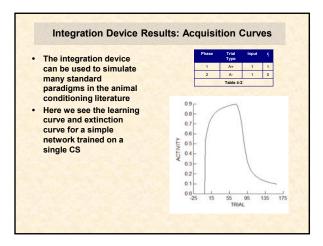


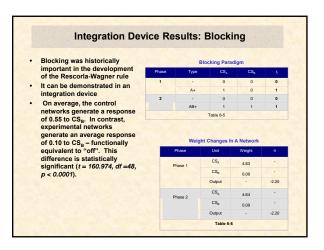












# **Empirical Equivalences**

- Dawson (2008) reports a number of experiments that have shown that integration devices can model many standard conditioning phenomena
  - Classical conditioning of individual stimuli
  - Behaviorally plausible acquisition and extinction curves
  - . The effect of CS intensity on the rate of conditioning
  - The effect of US intensity on the rate of conditioning
  - Associations to compound stimuli
  - The discrimination of compound stimuli from their components
  - Overshadowing
  - Blocking
  - · Conditioned inhibition
  - · Renewal, or context-dependent extinction
  - Superconditioning

### Formal Equivalence?

· Sutton and Barto proved the equivalence between a connectionist architecture and a psychological learning rule by translating the Rescorla-Wagner rule into the Widrow-Hoff rule



- · A similar proof has been developed by Gluck
- These proofs assume that the activation function of the output unit is linear!

#### **Linear Proof**

- If activity is identical to net input, and net input is total associative strength, then the error term in the delta rule is identical to the "distance from maximum association term" in the Rescorla-Wagner model
- That is, the Rescorla-Wagner model can be translated into the delta rule under this assumption

$$\Sigma V = V_A + V_B + V_C$$

$$\Sigma V = \sum_i a_i V_i$$

$$\Sigma V = \sum_i a_i V_i = \sum_i a_i W_{ij} = net_j$$

$$a_j = \sum_i a_i w_{ij} = net_j$$





#### **Nonlinear Activity and Association**

Perceptrons and related devices depend on nonlinear activation functions, so the typically cited proof of the relation between animal and machine learning is not really all that applicable



One proposal is the equation below:

We need to define how nonlinear output is related to internal associative strength

 $\Sigma V = \lambda \cdot f(net_i)$ 

#### **Nonlinear Proof**

$$\Delta V_{i(t)} = \alpha_i (\lambda \cdot US - \Sigma V_{(t)}) \cdot CS_i$$

$$\Delta V_{i(t)} = \alpha_i (\lambda \cdot US - \lambda \cdot f(net_j)_{(t)}) \cdot a_i$$

$$\Delta V_{i(t)} = \alpha_i \cdot \lambda \cdot (US - f(net_j)_{(t)}) \cdot a_i$$

$$= \alpha_i \cdot \lambda \cdot (US - a_{j(t)}) \cdot a_i$$

$$\Delta V_{i(t)} = \eta \cdot (US - a_{j(t)}) \cdot a_i$$

$$\Delta w_{ij} = \eta \cdot \delta_j \cdot a_i$$

$$= \eta \cdot (t_j - a_j) \cdot a_i$$

Simplify constants

If US indicates presence, then the equation above is identical to the delta rule, but now for a nonlinear system!

#### The Perceptron Paradox

- Miller, Barnet and Grahame (1995) have documented many successes and failures of the Rescorla-Wagner model
- Given the formal equivalence that we have established, perceptrons and integration devices must have the same successes and failures
- The perceptron paradox is that this is not true!
- We can easily demonstrate learning results in an integration device that diverge from the Rescorla-Wagner model, and in fact improve upon it





#### Paradoxical Result: Facilitated Reacquisition

- The Rescorla-Wagner model does not predict facilitated reacquisition after extinction
- This is one of the model's failures
- This failure is not evident in an integration device!
- On average, networks learned the associations to the CSs after 695.9 sweeps during Phase 1. After extinction, networks reacquired these associations after only 62.6 sweeps. Not surprisingly, this difference was statistically significant (t = 3005.415, df =48, p < 0.0001).

Phase	Trial Type	CS <sub>A</sub>	CS <sub>a</sub>	ţ
1		0	0	0
	A+	1	0	1
	B+	0	1	1
2		0	0	0
	A-	1	0	0
	B-	0	1	0
3		0	0	0
100	A+	1	0	1
	B+	0	1	1
Table 7-1				

#### Paradoxical Result: Extinction of a Conditioned Inhibitor

- The Rescorla-Wagner model predicts that when a conditioned inhibitor is extinguished, its associative strength should become more positive
- This is one of the model's failures, as this prediction is not supported by animal data
- This failure is not evident in an integration device!
- Note the changes in the conditioned inhibitor's weight after phase 2 training

Phase	Trial Type	CS <sub>A</sub>	CS <sub>a</sub>	
1	-	0	0	0
	A+	1	0	1
	AB-	1	1	0
2	-	0	0	0
	A-	1	0	0
	B-	0	1	0
Table 7-5				-11

Phase	Unit	Weight	
1	CS <sub>A</sub>	4.47	
	CS <sub>n</sub>	-4.80	
	Output		-2.45
2	CS <sub>A</sub>	2.37	-
	CS <sub>n</sub>	-4.81	-
	Output	-	-4.58

#### Paradoxical Result: Overexpectation

- Let CS<sub>A</sub> and CS<sub>B</sub> be independently paired with a US. Then, the two CSs are presented as a compound and are paired with the US.
- Overexpectation is defined as occurring when there is reduced responding (relative to a control) to CS<sub>A</sub> and CS<sub>B</sub> as individual stimuli following the training on the compound stimulus.
- Prediction of this effect was a triumph of the Rescorla-Wagner model
- Dawson and Spetch (2005) argued that the overexpectation effect will not be produced in an integration device, and supported this argument with simulation results





#### Why Does The Paradox Occur?

- The perceptron paradox arises because integration devices were not just mathematical models of changes in associative strength, but were simulations that had to behave Therefore, associative strength must be converted into a response The Rescorla-Wagner The perceptron
- The Rescorla-Wagner model is mute with respect to how associative strength becomes behavior

Property	Mathematical Models	Computer Simulations
Analyses of existing data	Yes	Possibly
Linear transformation	Usually not	Usually not
Goodness of fit	Yes	Yes, but nonstandard
Yields surprises	Maybe	Hopefully
Behaves	No	Yes

#### **Implications Of The Paradox**

- The Rescorla-Wagner model is evaluated by comparing it to behaving animals

  Such comparisons must involve a tacit theory of how associative strength becomes behavior!
- The nature of this theory has a severe impact on the responses of the model for instance, you can change the behavioral predictions of the model by changing your theory of behavior, but leaving Rescorla-Wagner untouched!
- For example, Dawson and Spetch (2005) have shown that changing the activation function has implications for whether overexpectation is observed. This change does not affect a "Rescorla-Wagner" account of machine learning!!

